

**CP**

**PURPOSE**

Compute the Process capability index ( $C_p$ ) for a variable.

**DESCRIPTION**

The process capability index measures the performance (i.e., the “capability”) of an industrial process and is defined as follows:

$$C_p = (USL - LSL)/(6s)$$

where USL and LSL are the upper and lower specification limits and  $s$  is the sample standard deviation. The USL and LSL are user defined limits within which a product is considered acceptable (values outside these limits indicate that a product is defective). Values less than 1 indicate that there are still some defectives in the process. A value of  $6s$  yields a range of plus or minus 3 standard deviations. For example, if the specification limits are symmetric about the mean of the data and the calculated  $C_p$  is exactly 1, this means that the specification limits fall at plus and minus 3 standard deviations from the mean and that the percentage of defectives will be approximately 1% (under a normality assumption). Values greater than 1 indicate the specification limits are even greater than 3 standard deviations from the mean (and so there will be less defectives) while values less than 1 indicate that the specification limits are less than 3 standard deviations from the mean (and so there will be more defectives).

**SYNTAX**

LET <par> = CP <y> <SUBSET/EXCEPT/FOR qualification>  
 where <y> is a response variable;  
 <par> is a parameter where the computed  $C_p$  index is stored;  
 and where the <SUBSET/EXCEPT/FOR qualification> is optional.

**EXAMPLES**

LET A = CP Y1  
 LET A = CP Y1 SUBSET TAG > 2

**NOTE 1**

Recall that Chebychev’s theorem states that at least 75% of a variables observations must fall within plus or minus 2 standard deviations of the mean and that at least 88% of them must fall within plus or minus 3 standard deviations. This is for any distribution. For a normal distribution, these numbers are 95.4% and 99.7% respectively.

**NOTE 2**

The upper and lower specification limits must be specified by the user as follows:

LET LSL = <value>  
 LET USL = <value>

**NOTE 3**

If your specification limits are not symmetric about the mean, the CPK statistic may be a better choice than the CP statistic. It is an alternate calculation of CP that adjusts for possibly nonsymmetric specification limits.

**DEFAULT**

None

**SYNONYMS**

None

**RELATED COMMANDS**

- CP PLOT = Generate a  $C_p$  versus subset plot.
- CONTROL CHART = Generate a control chart.
- CPK = Compute the  $C_{pk}$  index.
- PERCENT DEFECTIVE = Compute the percentage of defectives in a sample.
- EXPECTED LOSS = Compute the expected loss of a sample.

**REFERENCE**

“Guide to Quality Control,” Kaoru Ishikawa, Asian Productivity Organization, 1982 (chapter 13).

## APPLICATIONS

Quality Control

## IMPLEMENTATION DATE

90/12

## PROGRAM

SKIP 25

READ GEAR.DAT DIAMETER

LET LSL = 0.99

LET USL = 1.01

LET A = CP DIAMETER

The computed  $C_p$  value is 0.53.