

**GAMCDF****PURPOSE**

Compute the standard form of the gamma cumulative distribution function.

**DESCRIPTION**

The standard form of the gamma cumulative distribution function is:

$$F(x) = \frac{\Gamma_x(\gamma)}{\Gamma(\gamma)} \quad x \geq 0 \quad (\text{EQ 8-217})$$

where  $\gamma$  is a positive number that is the shape parameter and  $\Gamma$  and  $\Gamma_x$  are the complete gamma and incomplete gamma functions respectively. The mean and standard deviation of the standard gamma distribution are  $\gamma$  and  $\sqrt{\gamma}$  respectively.

**SYNTAX**

LET <y2> = GAMCDF(<y1>,<gamma>) <SUBSET/EXCEPT/FOR qualification>

where <y1> is a variable, a number, or a parameter;

<y2> is a variable or a parameter (depending on what <y1> is) where the computed gamma cdf value is saved;

<gamma> is a number or parameter that specifies the shape parameter;

and where the <SUBSET/EXCEPT/FOR qualification> is optional.

**EXAMPLES**

LET A = GAMCDF(3,1.5)

LET Y = GAMCDF(X1,GAMMA)

**NOTE 1**

The general form of the gamma cumulative distribution function is:

$$F(x) = \frac{\Gamma_{x-\mu}(\gamma)}{\Gamma(\gamma)} \quad x \geq 0 \quad (\text{EQ 8-218})$$

The parameter  $\mu$  is a location parameter and the parameter  $\beta$  is a scale parameter. See topic (3) under the General considerations section at the beginning of this chapter for a discussion of generating cdf values for the general form of the distribution.

**NOTE 2**

If  $\gamma$  is 1, this distribution reduces to the exponential distribution. If  $\gamma$  is a positive integer, the gamma distribution is called the Erlang distribution. The gamma distribution with  $\gamma = (v/2)$ ,  $\mu = 0$ , and  $\beta = 2$  where  $v$  is a positive integer is a chi-square distribution with  $v$  degrees of freedom.

**DEFAULT**

None

**SYNONYMS**

GAMMAIP

**RELATED COMMANDS**

GAMPDF	=	Compute the gamma probability density function.
GAMPPF	=	Compute the gamma percent point function.
EXPCDF	=	Compute the exponential cumulative distribution function.
EXPPDF	=	Compute the exponential probability density function.
EXPPPF	=	Compute the exponential percent point function.
CHSCDF	=	Compute the chi-square cumulative distribution function.
CHSPDF	=	Compute the chi-square probability density function.
CHSPPF	=	Compute the chi-square percent point function.

**REFERENCE**

“Continuous Univariate Distributions - 1,” Johnson and Kotz, Houghton Mifflin, 1970 (chapter 17).

“Handbook of Mathematical Functions, Applied Mathematics Series, Vol. 55,” Abramowitz and Stegun, National Bureau of Standards, 1964 (page 930).

## APPLICATIONS

Data Analysis, Reliability

## IMPLEMENTATION DATE

94/4

## PROGRAM

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MAJOR YTIC NUMBER 6
MINOR YTIC NUMBER 1
YLIMITS 0 1
YTIC DECIMAL 1
XLIMITS 0 5
XTIC OFFSET 0.6 0.6
SEGMENT 1 COORDINATES 16 88 21 88; SEGMENT 1 PATTERN SOLID
SEGMENT 2 COORDINATES 16 84 21 84; SEGMENT 2 PATTERN DASH
SEGMENT 3 COORDINATES 16 80 21 80; SEGMENT 3 PATTERN DOT
SEGMENT 4 COORDINATES 16 76 21 76; SEGMENT 4 PATTERN DA2
LEGEND 1 GAMMA = 1; LEGEND 1 COORDINATES 22 87
LEGEND 2 GAMMA = 0.5; LEGEND 2 COORDINATES 22 83
LEGEND 3 GAMMA = 2; LEGEND 3 COORDINATES 22 79
LEGEND 4 GAMMA = 5; LEGEND 4 COORDINATES 22 75
LINES SOLID DASH DOT DASH2
TITLE GAMCDF FOR VARIOUS VALUES OF GAMMA
YILABEL PROBABILITY; XILABEL X
PLOT GAMCDF(X,1) FOR X = 0.01 0.01 5.5 AND
PLOT GAMCDF(X,0.5) FOR X = 0.01 0.01 5.5 AND
PLOT GAMCDF(X,2) FOR X = 0.01 0.01 5.5 AND
PLOT GAMCDF(X,5) FOR X = 0.01 0.01 5.5

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